

**\*\*H**(b) Argue that for any  $x$ , the minimal deterministic finite automaton for  $\text{suf } x$  has exactly  $|x| + 1$  states.

**\*\*H**51. (Greibach) Let  $M$  be an NFA,  $A = L(M)$ . Starting with  $M$ , do the following:

- reverse the transitions and interchange start and final states to get an NFA for  $\text{rev } A$ ;
- determinize the resulting NFA by the subset construction, omitting inaccessible states;
- do the above two steps again.

Prove that the resulting automaton is the minimal DFA for  $A$ .

52. For each of the following finite automata:

- Give an equivalent minimal deterministic finite automaton. Don't forget to remove inaccessible states.
- Give an equivalent regular expression.

(a)

$$\rightarrow \begin{array}{l} 1F \\ 2F \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{array} \begin{array}{|c|c|} \hline a & b \\ \hline 2 & 5 \\ 1 & 4 \\ 7 & 2 \\ 5 & 7 \\ 4 & 3 \\ 3 & 6 \\ 3 & 1 \\ \hline \end{array}$$

(b)

$$\rightarrow \begin{array}{l} 1F \\ 2F \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{array} \begin{array}{|c|c|} \hline a & b \\ \hline 2 & 6 \\ 1 & 7 \\ 5 & 2 \\ 2 & 3 \\ 3 & 1 \\ 7 & 3 \\ 6 & 5 \\ \hline \end{array}$$

(c)

$$\rightarrow \begin{array}{l} 1 \\ 2F \\ 3 \\ 4F \\ 5 \\ 6F \\ 7 \end{array} \begin{array}{|c|c|} \hline a & b \\ \hline 1 & 3 \\ 6 & 3 \\ 5 & 7 \\ 6 & 1 \\ 1 & 7 \\ 2 & 7 \\ 5 & 3 \\ \hline \end{array}$$

(d)

$$\rightarrow \begin{array}{l} 1F \\ 2F \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{array} \begin{array}{|c|c|} \hline a & b \\ \hline 2 & 5 \\ 1 & 6 \\ 4 & 3 \\ 7 & 1 \\ 6 & 7 \\ 5 & 4 \\ 4 & 2 \\ \hline \end{array}$$